

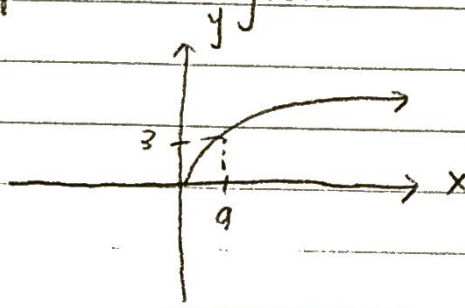
$$\sqrt{9}$$

$$3 \quad (\text{not } \pm 3)$$

Argument 1:

The square root is a function.

If we were to take  $y = \sqrt{x}$ , the graph would yield:



This is a function and passes the VLT. No graph represents an output of -3.

Argument 2:

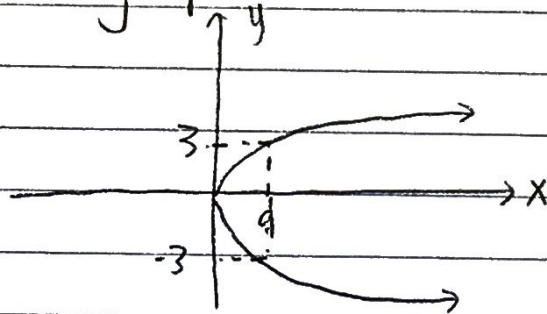
The counterexample may be if you take

$$y = \sqrt{x}$$

$$y^2 = x$$

(square both sides)

then your graph is



seemingly making output 3, -3.

However, by squaring both sides, you introduce the negative outputs as **EXTRANEOUS SOLUTIONS**, which in fact are not solutions.

Argument 3: The counterexample that

$$\frac{\sqrt{9}}{\sqrt{(3)^2}} \quad \sqrt{(-3)^2}$$
$$3 \quad -3$$

that the square and square root are inverse operations.

BUT

using laws of exponents, I can rewrite  $\sqrt{(-3)^2}$  as  $(\sqrt{-3})^2$  which defies the restriction that there must be a non-negative number under the radical.

Argument 4 (this is in Holt)

$\sqrt[n]{x^n}$  where  $n$  is even

$|x|$

$$\text{so } \sqrt{3^2} \quad \sqrt{(-3)^2}$$
$$|3| \quad |-3|$$
$$3 \quad 3$$

Argument 5: if  $\sqrt{9} = \pm 3$ , what does  $\pm\sqrt{9}$  yield? By convention, there is an invisible  $+$  in front of  $\sqrt{9}$ , yielding only 3.

Argument 6:  $y^2 = x$  solicits 2 real number answers because  $y$  has a degree of 2, where as  $y = \sqrt{x}$  only solicits 1 answer because

Argument 7: In the case of  $x^2 = 9$ , (same as argument 6)

$$\sqrt{x^2} = \sqrt{9}$$

$$x = \pm \sqrt{9}$$

$x = \pm 3$  in this equation form but only because (argument 5), there is a need for the notation  $\pm$

Argument 8: The square root sign  $\sqrt{\quad}$  is referred to as the principal square root (aka, the primary square root, positive square root) meaning  $\sqrt{9}$  is 3 (only the positive value).

Argument 9: Lines 182 and 183 of the California State Standards of Mathematics for Grade 8 say so. 😊